
Multiple-choice examination in: GRA 60352 Mathematics

Examination date:	24.05.2011, 09:00 – 10:00
Permitted examination aids:	Bilingual dictionary. BI-approved exam calculator: TEXAS INSTRUMENTS BA II Plus™
Answer sheets:	Answer sheet for multiple choice examinations
Total number of pages:	5
Number of attachments:	1 (example of how to use the answer sheet)

PLEASE READ THE FOLLOWING BEFORE YOU BEGIN!

- Students must themselves assure that the examination papers are complete.
- Students must provide the following information on the answer sheet:
 - Examination code
 - Personal initials
 - ID number

The student registration number must be recorded with both the appropriate numbers and by putting an “X” by the corresponding number in the columns below.

- Pens with green ink and pencils cannot be used in filling in answer sheets. Answer sheets must not be used for writing rough drafts.
- **All answers must be recorded with an “X” under the letter you believe corresponds with the correct answer.**
- **Cancel an “X” by filling in the box completely (boxes that are completely filled in will not be registered). “X” in two boxes for one question will be registered as a wrong answer.**
- The attached example shows you how the answer sheet would be filled in if A were the correct answer for question 1, B correct for question 2, C correct for question 3 and D correct for question 4. An “X” under E indicates that you choose not to answer question 5.
- **Your answers are to be recorded on the answer sheet. Answers written on the examination papers and not on the answer sheets will not be graded.**
- There is only one right answer for each question. Because the questions are weighted equally, it can be to your advantage to answer the simplest questions first.
- Wrong answers are given -1 point, unanswered questions get 0 points (indicated by an “X” next to E”) and correct answers are given 3 points.
- You can keep the examination papers.

Good luck!

This exam has 8 questions

QUESTION 1.

Consider the linear system

$$\begin{pmatrix} 1 & 2 & -3 & -1 & 0 \\ 0 & 1 & 7 & 3 & -4 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \end{pmatrix} = \begin{pmatrix} 3 \\ 0 \\ 2 \\ 1 \end{pmatrix}$$

Which statement is true?

- (A) The linear system is inconsistent
- (B) The linear system has a unique solution
- (C) The linear system has one degree of freedom
- (D) The linear system has two degrees of freedom
- (E) I prefer not to answer.

QUESTION 2.

Consider the set of vectors $\mathcal{B} = \{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\}$, where

$$\mathbf{v}_1 = \begin{pmatrix} 2 \\ 3 \\ -1 \end{pmatrix}, \quad \mathbf{v}_2 = \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix}, \quad \mathbf{v}_3 = \begin{pmatrix} h+1 \\ h \\ h-2 \end{pmatrix}$$

and h is a parameter. Which statement is true?

- (A) \mathcal{B} is a linearly independent set of vectors for all h
- (B) \mathcal{B} is a linearly independent set of vectors exactly when $h = 0$
- (C) \mathcal{B} is a linearly independent set of vectors exactly when $h \neq 5$
- (D) \mathcal{B} is a linearly independent set of vectors exactly when $h \neq -1$
- (E) I prefer not to answer.

QUESTION 3.

Compute the rank of the matrix

$$A = \begin{pmatrix} 2 & 10 & 6 & 8 \\ 1 & 5 & 4 & 11 \\ 3 & 15 & 7 & -2 \end{pmatrix}$$

Which statement is true?

- (A) $\text{rk } A = 1$
- (B) $\text{rk } A = 2$
- (C) $\text{rk } A = 3$
- (D) $\text{rk } A = 4$
- (E) I prefer not to answer.

QUESTION 4.

Consider the matrix

$$A = \begin{pmatrix} 3 & 1 \\ -2 & 6 \end{pmatrix}$$

Which statement is true?

- (A) A has eigenvalues $\lambda = 2$ and $\lambda = -1$
- (B) A has eigenvalues $\lambda = 2$ and $\lambda = 7$
- (C) A has a single eigenvalue $\lambda = 3$
- (D) A has eigenvalues $\lambda = 4$ and $\lambda = 5$
- (E) I prefer not to answer.

QUESTION 5.

Consider the matrix A and the vector \mathbf{v} given by

$$A = \begin{pmatrix} 2 & 1 \\ -1 & 3 \end{pmatrix}, \quad \mathbf{v} = \begin{pmatrix} 1 \\ b \end{pmatrix}$$

Which statement is true?

- (A) The vector \mathbf{v} is not an eigenvector for A
- (B) The vector \mathbf{v} is an eigenvector for A when $b = -1$
- (C) The vector \mathbf{v} is an eigenvector for A when $b \geq 0$
- (D) The vector \mathbf{v} is an eigenvector for A for all b
- (E) I prefer not to answer.

QUESTION 6.

Consider the quadratic form

$$Q(x_1, x_2) = -2x_1^2 + 12x_1x_2 + 2x_2^2$$

Which statement is true?

- (A) Q is positive semidefinite but not positive definite
- (B) Q is negative semidefinite but not negative definite
- (C) Q is indefinite
- (D) Q is positive definite
- (E) I prefer not to answer.

QUESTION 7.

Consider the function

$$f(x_1, x_2, x_3) = -x_1^2 + 2x_1x_2 - 3x_2^2 - x_3^2 - x_1 - x_3$$

defined on \mathbb{R}^3 . Which statement is true?

- (A) f is a convex function but not a concave function
- (B) f is a convex function and a concave function
- (C) f is not a convex function but a concave function
- (D) f is neither a convex nor a concave function
- (E) I prefer not to answer.

QUESTION 8.

Consider the matrix power A^7 of the matrix

$$A = \begin{pmatrix} 1 & 2 \\ 0 & -1 \end{pmatrix}$$

Which statement is true?

- (A) $A^7 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
- (B) $A^7 = \begin{pmatrix} 1 & 2 \\ 0 & -1 \end{pmatrix}$
- (C) $A^7 = \begin{pmatrix} 3 & -2 \\ 4 & 1 \end{pmatrix}$
- (D) $A^7 = \begin{pmatrix} 1 & 128 \\ 0 & -1 \end{pmatrix}$
- (E) I prefer not to answer.